
Design LIGNATUR element**Pos.110.0. 001**

Decisive building regulations

EN 1991, EN 1995

Object: Example School
Component: Floor above ground floor
Description -
Project-No. 2021'0017

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Date:

2021-06-29

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Load hypothesis

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Permanent actions

			0.00 kN/m ²
Floor structure	Cement screed 60mm (22kN/m ³ * 0.060m)		1.32 kN/m ²
Noise insulation board	Trittschalldämmung Mineralfaser 40mm (s' ≤ 7 MN/m ³)		0.04 kN/m ²
Weight	Elastisch gebundene Schüttung 80mm (15kN/m ³ * 0.080m)		1.20 kN/m ²
	-		0.00 kN/m ²
LIGNATUR surface element LFE t=40	g + 0.00		0.62 kN/m ²
	-		0.00 kN/m ²
		g_k=	3.18 kN/m²

Variable actions

C1 - Areas with tables			3.00 kN/m ²
Lightweight separating walls (< 3 kN/m)			0.80 kN/m ²
		q_k=	3.80 kN/m²

Partial safety factors for actions in different design situations

Partial safety factor			
- permanent actions		Y _g =	1.35 ()
- permanent actions	Accidental design situation	Y _{g,A} =	1.00 ()
- variable actions		Y _q =	1.50 ()
Factor for combination value			
- rare		Ψ ₀ =	0.70 ()
- frequent		Ψ ₁ =	0.70 ()
- quasi permanent		Ψ ₂ =	0.60 ()
Deformation factor		k _{def} =	0.60 ()

Ultimate limit state

Permanent action	Y _g *g _k	=	4.29 kN/m ²
Permanent + variable action	Y _g *g _k +Y _q *q _k	=	9.99 kN/m ²

Ultimate limit state in fire

Permanent + variable action	Y _{g,A} *g _k +Ψ ₂ *q _k	=	5.46 kN/m ²
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Serviceability limit state

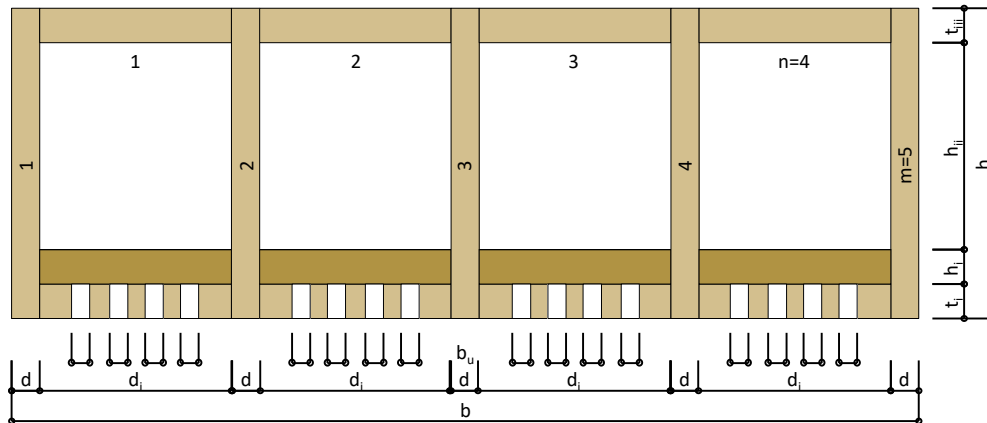
Permanent + variable action, inst	g _k +q _k	=	6.98 kN/m ²
Permanent + variable action, fin	g _k *(1+k _{def})+q _k (1+Ψ ₂ *k _{def})	=	10.25 kN/m ²

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Cross section characteristics

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Cross section

Element type	LIGNATUR surface element LFE t=40	L40
Fire resistance	REI60	REI60
Sound insulation	-	0
Thermal insulation	-	
Absorption	Acoustics type 3.1	3.1

Parameter

Height		h=	360 mm
Width		b=	1000 mm
Number of webs		m=	5 ()
Thickness of web		d=	31 mm
Number of cavities	m-1	n=	4 ()
Width of hollow space	(b-m*d)/n	d_i=	211 mm
Thickness upper lamella		t_iii=	40 mm
Thickness middle lamella		t_ii=	0 mm
Thickness lower lamella		t_i=	40 mm
Filling opening		b_o=	0 mm
Ø Filling opening		b_o,w=	0 mm
Perforation acoustics type 3.1 in lower lamella	n*4*20	b_u=	320 mm
Ø Perforation acoustics type 3.1 in lower lamella	n*4*20	b_u,w=	320 mm
Height of hollow space	h-t_iii-t_ii-h_i-t_i	h_ii=	240 mm
Wood fibre absorber thickness		h_i=	40 mm

Densities

Spruce wood		ρ _{Holz} =	4.70 kN/m ³
Insulation in the hollow space	Air=0kg/m3	ρ _{Isolation} =	0.00 kN/m ³
Wood fibre absorber	Air=0kg/m3	ρ _{Absorber} =	1.10 kN/m ³

Cross section areas

Wood gross (self-weight)	$b \cdot h - (n \cdot d_i) \cdot (h_{ii} + h_i)$	$A_b =$	123400 mm ²
Wood net (ultimate limit state)	$b \cdot h - (n \cdot d_i) \cdot (h_{ii} + h_i) - b_o \cdot t_{iii} - b_u \cdot t_i$	$A_n =$	110'600 mm ²
Wood Ø (serviceability limit state)	$b \cdot h - (n \cdot d_i) \cdot (h_{ii} + h_i) - b_{o,w} \cdot t_{iii} - b_{u,w} \cdot t_i$	$A_{\emptyset} =$	110'600 mm ²
Hollow space	$(b - m \cdot d) \cdot h_{ii}$	$A_K =$	202'800 mm ²
Wood fibre absorber	$(b - m \cdot d) \cdot h_i$	$A_A =$	33'800 mm ²

Self-weight

LIGNATUR element	$(A_b \cdot \rho_{Holz} + A_K \cdot \rho_{Isolation} + A_A \cdot \rho_{Absorber}) / 1000^2 / b \cdot 1000$	$g =$	0.62 kN/m ²
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Center of gravity Z coordinates in Y direction

Wood net	$(m \cdot d \cdot h^2 / 2 + (n \cdot d_i - b_u) \cdot t_i^2 / 2 + n \cdot d_i \cdot t_{ii} \cdot (t_i + h_i + t_{ii} / 2) + (n \cdot d_i - b_o) \cdot t_{iii} \cdot (h - t_{iii} / 2)) / A_n$	$S_y =$	199 mm
Wood Ø	$(m \cdot d \cdot h^2 / 2 + (n \cdot d_i - b_{u,w}) \cdot t_i^2 / 2 + n \cdot d_i \cdot t_{ii} \cdot (t_i + h_i + t_{ii} / 2) + (n \cdot d_i - b_{o,w}) \cdot t_{iii} \cdot (h - t_{iii} / 2)) / A_{\emptyset}$	$S_{y,\emptyset} =$	199 mm

Moments of inertia in case of fire

Wood net	$m \cdot d \cdot h^3 / 12 + m \cdot d \cdot h \cdot (h/2 - s_y)^2 + (n \cdot d_i - b_u) \cdot t_i^3 / 12 + (n \cdot d_i - b_u) \cdot t_i \cdot (s_y - t_i / 2)^2 + n \cdot d_i \cdot t_{ii}^3 / 12 + n \cdot d_i \cdot t_{ii} \cdot (s_y - t_i - h_i - t_{ii} / 2)^2 + (n \cdot d_i - b_o) \cdot t_{iii}^3 / 12 + (n \cdot d_i - b_o) \cdot t_{iii} \cdot (h - s_y - t_{iii} / 2)^2$	$I_y =$	1'974'903'484 mm ⁴
Wood Ø	$m \cdot d \cdot h^3 / 12 + m \cdot d \cdot h \cdot (h/2 - s_y)^2 + (n \cdot d_i - b_{u,w}) \cdot t_i^3 / 12 + (n \cdot d_i - b_{u,w}) \cdot t_i \cdot (s_y - t_i / 2)^2 + n \cdot d_i \cdot t_{ii}^3 / 12 + n \cdot d_i \cdot t_{ii} \cdot (s_y - t_i - h_i - t_{ii} / 2)^2 + (n \cdot d_i - b_{o,w}) \cdot t_{iii}^3 / 12 + (n \cdot d_i - b_{o,w}) \cdot t_{iii} \cdot (h - s_y - t_{iii} / 2)^2$	$I_{y,\emptyset} =$	1'974'903'484 mm ⁴

Resistance moment

Wood net	I_y / S_y	$W_y =$	9'948'275 mm ³
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Bending stiffness

Wood Ø	$E_{0,mean} \cdot I_{y,\emptyset}$	$EI_{\emptyset} =$	21.724 * 10 ¹² Nmm ²
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Static moment of area

Wood net $t_i + h_i + t_{ii} < s_y \leq h - t_{iii}$	$m \cdot d \cdot (h - s_y)^2 / 2 + (n \cdot d_i - b_o) \cdot t_{iii} \cdot (h - s_y - t_{iii} / 2)$	$S_y =$	6'803'064 mm ³
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Shear surface

Wood net	$m \cdot d \cdot I_y / S_y$	$A_w =$	44'996 mm ²
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Characteristic properties

Strength class				C24
Bending	$f_{m,k} \cdot k_{mod} / \gamma_m$	$f_{m,k} =$	24 N/mm ²	$f_{m,d} =$ 16.6 N/mm ²
Tension parallel to the grain	$f_{t,0,k} \cdot k_{mod} / \gamma_m \cdot 20$	$f_{t,0,k} =$	14 N/mm ²	$f_{t,0,d} =$ 9.7 N/mm ²
Tension perpendicular to the grain	$f_{t,90,k} \cdot k_{mod} / \gamma_m$	$f_{t,90,k} =$	0.4 N/mm ²	$f_{t,90,d} =$ 0.3 N/mm ²
Compression parallel to the grain	$f_{c,0,k} \cdot k_{mod} / \gamma_m$	$f_{c,0,k} =$	21 N/mm ²	$f_{c,0,d} =$ 14.5 N/mm ²
Compression perpendicular to the grain	$f_{c,90,k} \cdot k_{mod} / \gamma_m$	$f_{c,90,k} =$	2.5 N/mm ²	$f_{c,90,d} =$ 1.7 N/mm ²
Shear	$f_{v,k} \cdot k_{mod} / \gamma_m$	$f_{v,k} =$	2.0 N/mm ²	$f_{v,d} =$ 1.4 N/mm ²
Modulus of elasticity parallel			$E_{0,mean} =$	11'000 N/mm ²
Modification factor			$k_{mod} =$	0.9 ()
Partial safety factor			$\gamma_m =$	1.3 ()

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Ultimate limit state, serviceability limit state

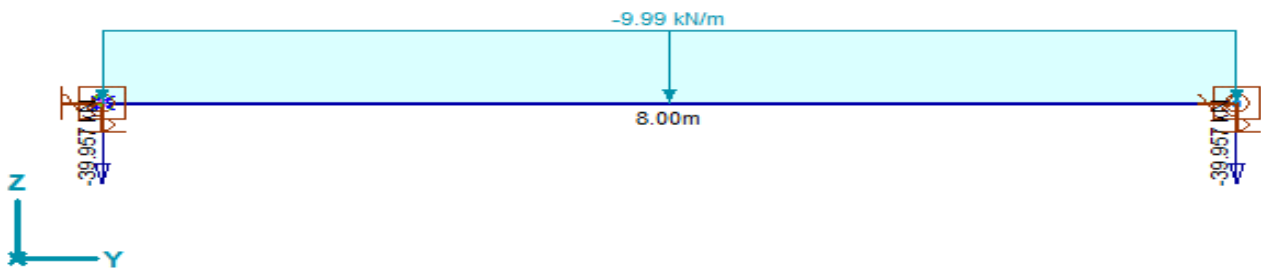
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Decisive building regulations EN 1991, EN 1995

Calculation with AxisVM

Structural system in ultimate limit state

1-span beam



Span length S1

$l_{s1} = 8'000$ mm

Moment diagram

Maximum moment

$M_{y,d} = 79.9$ kNm

Maximum bending stress

$M_{y,d} * 1000000 / (I_y / (h - s_y)) / 1000 * b$

$\sigma_{o,d} = 6.5$ N/mm²

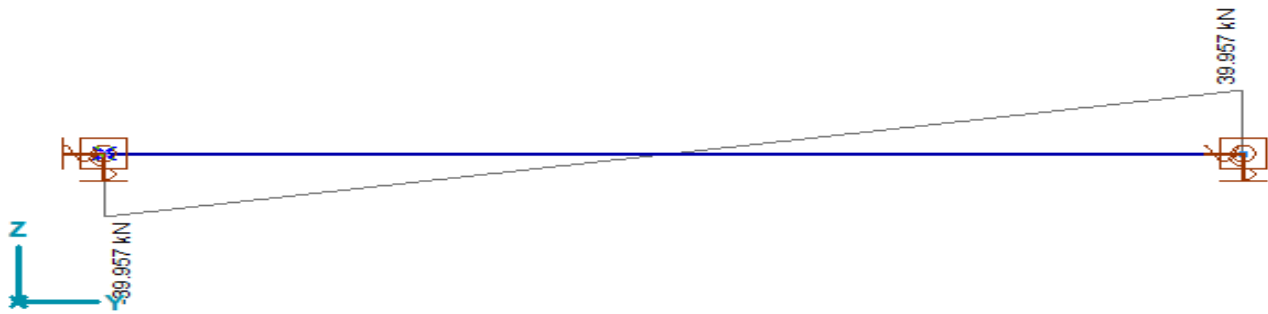
$M_{y,d} * 1000000 / (I_y / s_y) / 1000 * b$

$\sigma_{u,d} = 8.0$ N/mm²

$MAX(\sigma_{o,d}; \sigma_{u,d}) / f_{m,d}$

0.48 ≤ 1

Shear diagram



Maximum shear force

Maximum shear stress

$$V_{z,d} \cdot 1000 / A_w / 1000 \cdot b$$

$$\tau_d / f_{v,d}$$

$V_{z,d} =$

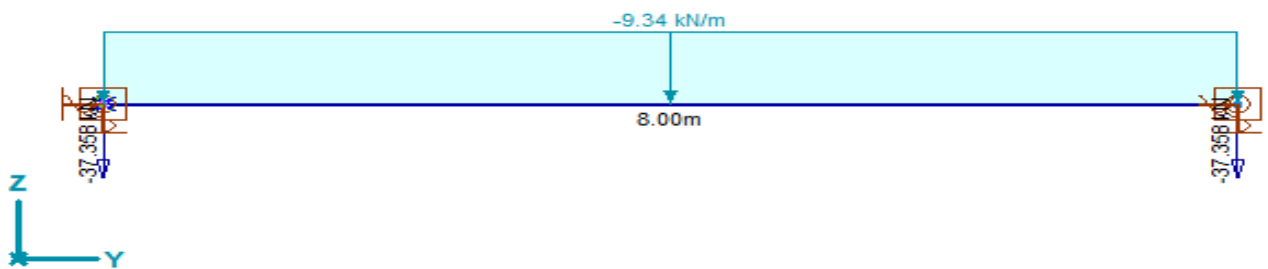
$\tau_d =$

40.0 kN

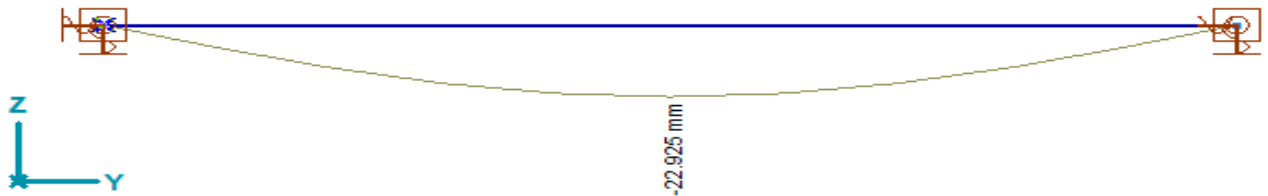
0.9 N/mm²

0.64 ≤ 1

Structural system in serviceability limit state for frequent combination



Deflection



Maximum deflections

$W_{z,inst,S1} =$

$W_{z,fin,S1} =$

$$I_{S1} / W_{z,inst,S1}$$

$$I_{S1} / W_{z,fin,S1}$$

17.1 mm

467 ≥ 400

25.2 mm

318 ≥ 300

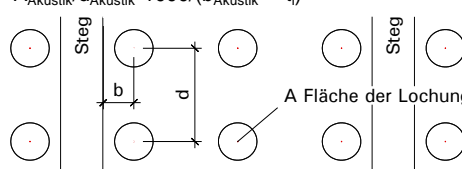
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Cross section characteristics in fire

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 ETA-11/0137 for LIGNATUR elements

Effective charring depth in fire

Duration of fire exposure		$t =$	60 min.
- charring time in slat t_i	$t_i/\beta_1 \leq t$	$t_1 =$	46 min.
- charring time in wood fibre absorber h_i	$h_i/\beta_2 \leq t - t_1$	$t_2 =$	14 min.
- charring time in slat t_{ii}	$t_{ii}/\beta_3 \leq t - t_1 - t_2$	$t_3 =$	0 min.
- charring time in thermal insulation h_{ii}	$h_{ii}/\beta_4 \leq t - t_1 - t_2 - t_3$	$t_4 =$	0 min.
Charring rate in slat t_i	Acoustics $0.22 * k + 0.72$	$\beta_1 =$	0.86 mm/min.
Factor (IBK report no. 283 ETH Zurich)	$A_{Akustik}/d_{Akustik} * 1000 / (b_{Akustik}^{1.5 * t_i})$	$k =$	0.65 ()
Surface of holes or slits		$A_{Akustik} =$	314 mm ²
Distance between holes or between slits		$d_{Akustik} =$	40 mm
Distance between holes or slits and web		$b_{Akustik} =$	45 mm
Charring rate in wood fibre absorber h_i	$0.9 * (450/\rho_{Absorber})^{1/2}$	$\beta_2 =$	1.82 mm/min.
Charring rate in slat t_{ii}		$\beta_3 =$	0.00 mm/min.
Charring rate in thermal insulation h_{ii}		$\beta_4 =$	0.00 mm/min.
Charred layer	$t_1 * \beta_1 + t_2 * \beta_2 + t_3 * \beta_3 + t_4 * \beta_4$	$d_{char} =$	65 mm
Condiseration of loss of strength		$d_{red} =$	7 mm
Effective charring depth	$d_{char} + d_{red}$	$d_{ef} =$	72 mm

Parameters in fire

Height	$h - d_{ef}$	$h_{fi} =$	288 mm
Width	b	$b_{fi} =$	1'000 mm
Number of webs	m	$m_{fi} =$	5 ()
Thickness of web	d	$d_{fi} =$	31 mm
Number of cavities	$n - 1$	$n_{fi} =$	4 ()
Width of hollow space	$(b_{fi} - m_{fi} * d_{fi}) / n_{fi}$	$d_{i,fi} =$	211 mm
Thickness upper lamella	$t_{iii} \geq t_i + h_i + t_{ii} + h_{ii} + t_{iii} - d_{ef} \geq 0$	$t_{iii,fi} =$	40 mm
Thickness middle lamella	$t_{ii} \geq t_i + h_i + t_{ii} - d_{ef} \geq 0$	$t_{ii,fi} =$	0 mm
Thickness lower lamella	$t_i - d_{ef} \geq 0$	$t_{i,fi} =$	0 mm
Filling opening	b_o	$b_{o,fi} =$	0 mm
Perforation acoustics type 3.1 in lower lamella	b_u	$b_{u,fi} =$	320 mm
Height of hollow space	$h_{ii} \geq t_i + h_i + t_{ii} + h_{ii} - d_{ef} \geq 0$	$h_{ii,fi} =$	240 mm
Wood fibre absorber thickness	$h_i \geq t_i + h_i - d_{ef} \geq 0$	$h_{i,fi} =$	8 mm

Cross sectional area in fire

Wood net (ultimate limit state) $b_{fi} \cdot h_{fi} - (n_{fi} \cdot d_{i,fi}) \cdot (h_{ii,fi} + h_{i,fi}) - b_{o,fi} \cdot t_{iii,fi} - b_{u,fi} \cdot t_{i,fi}$ $A_{n,fi} = 78'462 \text{ mm}^2$

Center of gravity Z coordinates in Y direction in fire

Wood net $(m_{fi} \cdot d_{fi} \cdot h_{fi}^2 / 2 + (n_{fi} \cdot d_{i,fi} - b_{u,fi}) \cdot t_{i,fi}^2 / 2 + n_{fi} \cdot d_{i,fi} \cdot t_{ii,fi} \cdot (t_{i,fi} + h_{i,fi} + t_{ii,fi} / 2) + (n_{fi} \cdot d_{i,fi} - b_{o,fi}) \cdot t_{iii,fi} \cdot (h_{fi} - t_{iii,fi} / 2)) / A_{n,fi}$ $S_{y,fi} = 198 \text{ mm}$

Moment of inertia in case of fire

Wood net $m_{fi} \cdot d_{fi}^3 / 12 + m_{fi} \cdot d_{fi} \cdot h_{fi} \cdot (h_{fi} / 2 - s_{y,fi})^2 + (n_{fi} \cdot d_{i,fi} - b_{u,fi}) \cdot t_{i,fi}^3 / 12 + (n_{fi} \cdot d_{i,fi} - b_{u,fi}) \cdot t_{i,fi} \cdot (s_{y,fi} - t_{i,fi} / 2)^2 + n_{fi} \cdot d_{i,fi} \cdot t_{ii,fi}^3 / 12 + n_{fi} \cdot d_{i,fi} \cdot t_{ii,fi} \cdot (s_{y,fi} - t_{i,fi} - h_{i,fi} - t_{ii,fi} / 2)^2 + (n_{fi} \cdot d_{i,fi} - b_{o,fi}) \cdot t_{iii,fi}^3 / 12 + (n_{fi} \cdot d_{i,fi} - b_{o,fi}) \cdot t_{iii,fi} \cdot (h_{fi} - s_{y,fi} - t_{iii,fi} / 2)^2$ $I_{y,fi} = 609'685'643 \text{ mm}^4$

Static moment of area in fire

Wood net $t_{i,fi} + h_{i,fi} + t_{ii,fi} < s_{y,fi} \leq h_{fi} - t_{iii,fi}$ $m_{fi} \cdot d_{fi} \cdot (h_{fi} - s_{y,fi})^2 / 2 + (n_{fi} \cdot d_{i,fi} - b_{o,fi}) \cdot t_{iii,fi} \cdot (h_{fi} - s_{y,fi} - t_{iii,fi} / 2)$ $S_{y,fi} = 3'023'564 \text{ mm}^3$
 $S_{y,fi} = 3'023'564 \text{ mm}^3$

Shear surface in fire

Wood net $m_{fi} \cdot d_{fi} \cdot I_{y,fi} / S_{y,fi}$ $A_{w,fi} = 31'255 \text{ mm}^2$

Characteristic properties in fire

Strength class C24

Bending $f_{m,k} \cdot k_{fi} / \gamma_{m,fi}$ $f_{m,d,fi} = 30.0 \text{ N/mm}^2$

Tension parallel to the grain $f_{t,0,k} \cdot k_{fi} / \gamma_{m,fi}$ $f_{t,0,d,fi} = 17.5 \text{ N/mm}^2$

Compression parallel to the grain $f_{c,0,k} \cdot k_{fi} / \gamma_{m,fi}$ $f_{c,0,d,fi} = 26.3 \text{ N/mm}^2$

Shear $f_{v,k} \cdot k_{fi} / \gamma_{m,fi}$ $f_{v,d,fi} = 2.5 \text{ N/mm}^2$

Factor for the determination of the 20th percentile $k_{fi} = 1.25 ()$

Partial safety factor $\gamma_{m,fi} = 1.0 ()$

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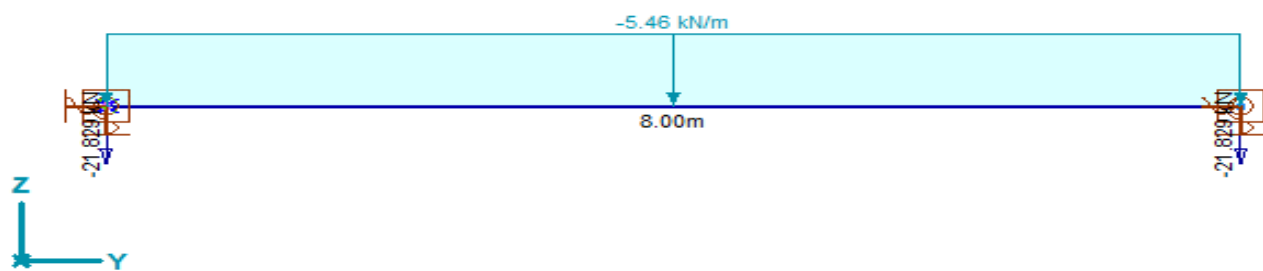
Ultimate limit state in case of fire

Pos.110.0. 001

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 ETA-11/0137 for LIGNATUR elements

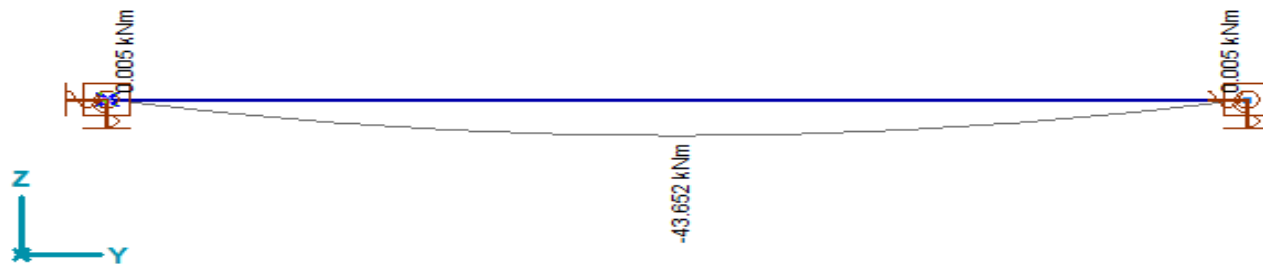
Calculation with AxisVM

Structural system in ultimate limit state in fire



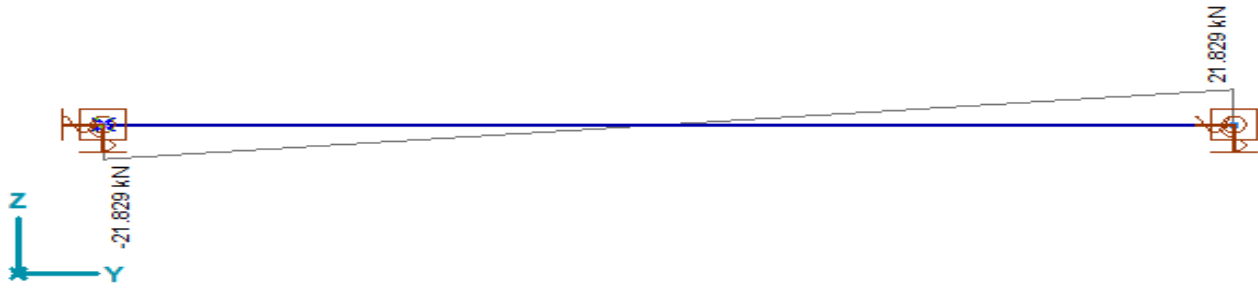
Span length S1 I_{S1}= 8'000 mm

Moment diagram in fire



Maximum moment		M _{y,d,fi} =	43.7 kNm
Maximum bending stress	$M_{y,d,fi} \cdot 1000000 / (I_{y,fi} / (h_{fi} - s_{y,fi})) / 1000 \cdot b_{fi}$	$\sigma_{o,d,fi}$ =	6.5 N/mm ²
	$M_{y,d,fi} \cdot 1000000 / (I_{y,fi} / s_{y,fi}) / 1000 \cdot b_{fi}$	$\sigma_{u,d,fi}$ =	14.1 N/mm ²
	$\text{MAX}(\sigma_{o,d,fi}, \sigma_{u,d,fi}) / f_{m,d,fi}$		0.47 ≤ 1

Shear diagram in fire



Maximum shear force
Maximum shear stress

$$V_{z,d,fi} \cdot 1000 / A_{w,fi} / 1000 \cdot b_{fi}$$

$$\tau_{d,fi} / f_{v,d,fi}$$

$V_{z,d,fi} =$ 21.8 kN
 $\tau_{d,fi} =$ 0.7 N/mm²
0.28 ≤ 1